

**QUESTION BANK**

<b>Title of the Subject: Engineering Mathematics-I</b>	
<b>Title of the Unit: Linear Algebra-Matrices</b>	<b>Unit No:- 1</b>

<b>Multiple Choice Questions</b>		
<b>Question No.</b>	<b>Question Description</b>	<b>Expected Marks</b>
<b>1</b>	If the rank of A is 2 then rank of A transpose is a)2    b)0    c)4    d) None of these	<b>1</b>
<b>2</b>	If the rank of A is 2 and the rank of B is 3 then the rank of AB is a)2    b)3    c)6    d) Depends on matrix AB	<b>1</b>
<b>3</b>	The rank of the matrix $A = \begin{bmatrix} 1 & 1 & -1 \\ 2 & -3 & 4 \\ 3 & -2 & 3 \end{bmatrix}$ is equal to a)2    b)3    c)1    d) None of these	<b>1</b>
<b>4</b>	The Eigen values of a triangular matrix are a) The elements of its principal diagonal      b) The elements of its non diagonal c) 0    d) None of these	<b>1</b>
<b>5</b>	Solving the equations $x + 2y + 3z = 0, 3x + 4y + 4z = 0, 7x + 10y + 12z = 0$ , we get a) $x = y = z = 0$ b) $x = y = z = 1$ c) $x = 1, y = 2, z = 3$ d) None	<b>1</b>
<b>6</b>	The eigen values of $A = \begin{bmatrix} 1 & 1 \\ 2 & 5 \end{bmatrix}$ are the roots of equation a) $\lambda^2 - 6\lambda + 3 = 0$ b) $\lambda^2 + 6\lambda + 3 = 0$ c) $\lambda^2 - 6\lambda - 3 = 0$ d) None	<b>1</b>

7	A square matrix A is said to be Orthogonal if a) $A = A^2$ b) $A' = A^{-1}$ c) $AA^{-1} = I$ d) None of these	1
8	The product of eigen values of a matrix $A = \begin{bmatrix} 2 & -3 \\ 4 & -2 \end{bmatrix}$ is a) 8    b) 4    c) 1    d) None of these	1
9	If $A = \begin{bmatrix} 3 & 2 \\ 1 & 4 \end{bmatrix}$ then $A(adjA)$ is equal to a) $\begin{bmatrix} 10 & 0 \\ 0 & 10 \end{bmatrix}$ b) $\begin{bmatrix} 0 & 10 \\ 10 & 0 \end{bmatrix}$ c) $\begin{bmatrix} 10 & 1 \\ 1 & 10 \end{bmatrix}$ d) None of these	1
10	If a matrix $A = \begin{bmatrix} x & 2 \\ 1 & x-1 \end{bmatrix}$ is singular then x is equal to a) 2,-1    b) 3,1    c) 0,1    d) None of these	1

### Short Answer Question

Question No.	Question Description	Expected Marks
1	Find the rank of $\begin{bmatrix} 1 & 2 \\ 2 & 3 \end{bmatrix}$ by converting to normal form.	2
2	Find rank of $A = \begin{bmatrix} 1 & 1 & 2 \\ 1 & 2 & 3 \\ 0 & -1 & 1 \end{bmatrix}$	2
3	Define normal form of matrix.	2
4	Find eigen values of matrix A , where: $A = \begin{bmatrix} 1 & 2 \\ 5 & 4 \end{bmatrix}$	2
5	Obtain characteristic equation of matrix $A = \begin{bmatrix} 1 & 0 & 2 \\ 0 & 2 & 1 \\ 2 & 0 & 3 \end{bmatrix}$	2
6	If the matrix form of system of non-homogeneous linear equation is $AX = D$ & $C = [A/D]$ then, discuss the condition of consistency of given system	2
7	Define rank of matrix and find rank by converting matrix A into canonical form $\begin{bmatrix} 1 & -1 & 2 \\ 4 & 2 & -1 \\ 2 & 2 & -2 \end{bmatrix}$ .	2
8	Find Eigen values for $\begin{bmatrix} 1 & 0 & -1 \\ 1 & 2 & 1 \\ 2 & 2 & 3 \end{bmatrix}$	2
9	Check the consistency $x + y + 3z = 0, x - y + z = 0, -x + 2y = 0$	2
10	Find rank of $A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 8 & 12 \\ -1 & 7 & 3 \end{bmatrix}$	2

Long Answer Question		
Question No.	Question Description	Expected Marks
1	<p>Determine the values of <math>\alpha</math> &amp; <math>\beta</math>, such that system of equation :</p> $x + y + z = 6, x + 2y + 3z = 10; x + 2y + \alpha z = \beta$ <p>has (i) no solution; (ii) unique solution</p> <p>(iii) infinite number of solution</p>	5
2	<p>find the value of <math>k</math> so that the system has the non-trivial solution</p> $8x - 4y - 6z = 0; 3x + y - kz = 0; 2x + 4y - z = 0.$	5
3	<p>Discuss the consistency of equation and hence solve</p> $x + 2y + 3z = 14, 2x - y + 3z = 8, 3x + y - 4z = 0$	5
4	<p>Find the rank of the matrix:</p> $\begin{bmatrix} 3 & 1 & 4 & 6 \\ 2 & 1 & 2 & 4 \\ 4 & 2 & 5 & 8 \\ 1 & 1 & 2 & 2 \end{bmatrix}$	5
5	<p>Find the Eigen vector for the lowest Eigen value for <math>\begin{bmatrix} 0 &amp; -1 &amp; -2 \\ 2 &amp; 3 &amp; 2 \\ 1 &amp; 1 &amp; 3 \end{bmatrix}</math>.</p>	5
6	<p>Solve:</p> $2x - 2y + 5z + 3w = 0; 4x - y + z + 2w = 0; 3x - 7y + 3z + 4w = 0; x - 3y + 3z + 3w = 0$	5
7	<p>Use Gauss –Jordan method to find inverse of the matrix</p> $\begin{bmatrix} 8 & 4 & -3 \\ 2 & 1 & 1 \\ 1 & 2 & 1 \end{bmatrix}$	5
8	<p>Test the consistency and solve if possible:</p> $x + y + z = 6; \quad x - y + 2z = 5;$ $3x + y + z = 8; \quad 2x - 2y + 3z = 7.$	5

9	Using the CALEY-HAMILTON theorem find the inverse of matrix : $\begin{bmatrix} 1 & 0 & 2 \\ 0 & 2 & 1 \\ 2 & 0 & 3 \end{bmatrix}$	5
10	Find the rank of the matrix by reducing to normal form $A = \begin{bmatrix} 1 & 3 & 4 & 2 \\ 2 & -1 & 3 & 2 \\ 3 & -5 & 2 & 2 \\ 6 & -3 & 8 & 6 \end{bmatrix}$	5



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### QUESTION BANK

<b>Title of the Subject: Engineering Mathematics-I</b>	
<b>Title of the Unit: Partial Differentiation</b>	<b>Unit No:- 2</b>

Multiple Choice Questions		
Question No.	Question Description	Expected Marks
1	If $u = x^3 + y^3$ then $\frac{\partial^2 u}{\partial x \partial y}$ is equal to a) 0    b) 3    c) -3    d) None of these	1
2	If $u = x^y$ then $\frac{\partial u}{\partial y}$ is equal to a) $x^y \log x$ b) 0    c) $y x^{y-1}$ d) None of these	1
3	If $z = \log(x^3 + y^3 - x^2y - xy^2)$ , then $x \frac{\partial z}{\partial x} + y \frac{\partial z}{\partial y}$ is equal to a) 3    b) 2    c) 0    d) None of these	1
4	$u = \frac{\sqrt{x} - \sqrt{y}}{\sqrt{x} + \sqrt{y}}$ is a homogeneous function of degree a) 0    b) 1    c) $\frac{1}{2}$ d) None of these	1

5	If $u = \cos^{-1}\left(\frac{x}{y}\right) + \tan^{-1}\left(\frac{y}{x}\right)$ , then $x^2 u_{xx} + 2xy u_{xy} + y^2 u_{yy}$ is equal to a) $u$ b) $2u$ c) 0    d) None of these	1
6	If $u = \log\left(\frac{x^2}{y}\right)$ , then $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y}$ is equal to a) $u$ b) $2u$ c) 1    d) None of these	1
7	If $u$ is a function of $x$ and $y$ , and $y$ is the function of $x$ , then which of the following is true? a) $\frac{du}{dx} = \frac{\partial u}{\partial t} + \frac{\partial u}{\partial y} \frac{dy}{dx}$ b) $\frac{du}{dx} = \frac{\partial u}{\partial x} + \frac{\partial u}{\partial y} \frac{dy}{dx}$ c) $\frac{du}{dx} = \frac{\partial u}{\partial x} + \frac{\partial u}{\partial t} \frac{dt}{dx}$ d) None	1
8	If $u = f(x, y) = c$ , then $\frac{dy}{dx}$ is equal to a) $-\frac{f_x}{f_y}$ b) $-\frac{f_y}{f_x}$ c) $\frac{f_x}{f_y}$ d) None of these	1
9	If $u = f\left(\frac{y}{x}\right)$ , then $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y}$ is equal to a) $2u$ b) $u$ c) 0    d) None of these	1
10	If $z = \sin^{-1}\left(\frac{x^2+y^2}{x+y}\right)$ , then $x \frac{\partial z}{\partial x} + y \frac{\partial z}{\partial y}$ is equal to a) 0    b) $\tan z$ c) $2 \tan z$ d) None of these	1

### Short Answer Question

Question No.	Question Description	Expected Marks
1	If $u = x \cdot \log(xy)$ where $x^3 + y^3 + 3xy = 1$ . Find $\frac{du}{dx}$	2
2	If $u = (x^2 + y^2 + z^2)$ Prove that, $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} + z \frac{\partial u}{\partial z} = 2u$ .	2
3	If $u = (1 - 2xy + y^2)^{-\frac{1}{2}}$ Find $\frac{\partial u}{\partial x}$	2
4	If $u = (1 - 2xy + y^2)^{-\frac{1}{2}}$ Find $\frac{\partial u}{\partial x}$	2
5	If $u = \log(x^2 + y^2)$ . Prove that, $\frac{\partial^2 u}{\partial x \partial y} = \frac{\partial^2 u}{\partial y \partial x}$	2
6	Find $\frac{dz}{dt}$ if $z = xy^2 + x^2y, x = at^2, y = 2at$	2
7	State Euler's theorem for a function $u$ of two variables	2
8	$u = \frac{x^3+y^3}{y\sqrt{x}}$ is a homogeneous function of degree $n = \dots\dots\dots$	2
9	Find $\frac{dy}{dx}$ , if $x^4 + y^4 = 5a^2xy$	2

10	If $u = x^2 + y^2 + z^2$ where $x = e^t, y = e^t \sin t, z = e^t \cos t$ Find $\frac{du}{dt}$	2
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Long Answer Question		
Question No.	Question Description	Expected Marks
1	Prove Euler's theorem for a function $u$ of two variables	5
2	If $u = \log(\tan x + \tan y + \tan z)$ then prove that, $\sin 2x \frac{\partial u}{\partial x} + \sin 2y \frac{\partial u}{\partial y} + \sin 2z \frac{\partial u}{\partial z} = 2$ .	5
3	If $z(x+y) = x^2 + y^2$ then show that, $\left\{\frac{\partial z}{\partial x} - \frac{\partial z}{\partial y}\right\}^2 = 4 \left[1 - \frac{\partial z}{\partial x} - \frac{\partial z}{\partial y}\right]$ .	5
4	If $u = ax + by, v = bx - ay$ , then find the value of $\left(\frac{\partial x}{\partial u}\right)_v \cdot \left(\frac{\partial x}{\partial v}\right)_u$ .	5
5	If $u = \sin^{-1}\left(\frac{x+y}{\sqrt{x}+\sqrt{y}}\right)$ Prove that, $x^2 \frac{\partial^2 u}{\partial x^2} + 2xy \frac{\partial^2 u}{\partial x \partial y} + y^2 \frac{\partial^2 u}{\partial y^2} = \frac{-\sin u \cdot \cos 2u}{4 \cos^3 u}$	5
6	If $z = f(u, v)$ , where $u = x \cos \theta - y \sin \theta, v = x \sin \theta + y \cos \theta$ , show that $x \frac{\partial z}{\partial x} + y \frac{\partial z}{\partial y} = u \frac{\partial z}{\partial u} + v \frac{\partial z}{\partial v}$	5
7	If $u = \log(x^3 + y^3 - x^2 y - xy^2)$ , Prove that, $x^2 \frac{\partial^2 u}{\partial x^2} + 2xy \frac{\partial^2 u}{\partial x \partial y} + y^2 \frac{\partial^2 u}{\partial y^2} = -3$ .	5
8	If $z = f(x, y), x = e^u + e^v, y = e^u - e^v$ . Prove that, $\frac{\partial z}{\partial u} - \frac{\partial z}{\partial v} = x \frac{\partial z}{\partial x} - y \frac{\partial z}{\partial y}$ .	5
9	Find $\frac{dy}{dx}$ , if $x^4 + y^4 = 5a^2 xy$	5
10	If $u = x^2 + y^2 + z^2$ where $x = e^t, y = e^t \sin t, z = e^t \cos t$ Find $\frac{du}{dt}$ .	5



QUESTION BANK

Title of the Subject: Engineering Mathematics-I	
Title of the Unit: Applications of Partial Differentiation	Unit No:- 3

Multiple Choice Questions		
Question No.	Question Description	Expected Marks
1	If $J_1 = \frac{\partial(u,v)}{\partial(x,y)}$ and $J_2 = \frac{\partial(x,y)}{\partial(u,v)}$ then $J_1 J_2$ is equal to a) 1    b) -1    c) 0    d) None of these	1
2	If $r = \frac{\partial^2 f}{\partial x^2}$ , $s = \frac{\partial^2 f}{\partial x \partial y}$ and $t = \frac{\partial^2 f}{\partial y^2}$ , then the condition for saddle point is a) $rt - s^2 < 0$ b) $rt - s^2 > 0$ c) $rt - s^2 = 0$ d) None of these	1
3	If $x = uv, y = \frac{u}{v}$ then $J = \dots\dots\dots$ a) $\frac{-2u}{v}$ b) $\frac{2u}{v}$ c) $\frac{u}{v}$ d) 0	1
4	If $x = r \cos \theta$ , $y = r \sin \theta$ then the Jacobian of the given transformation is a) $2r$ b) $r$ c) $\frac{1}{r}$ d) 0	1
5	The stationary point of the function $f(x, y) = x^3 + 3x^2y - 15x^2 - 15y^2 + 72x$ are a) (0,3) and (6,0)    b) (4,0) and (6,0)    c) (4,0) and (0,3)    d) None	1
6	The first two terms of Maclaurin's series expansion of $f(x, y) = e^x \sin y$ is a) $y + xy$ b) $xy + \frac{x^2}{2}$ c) $2x^2y + xy$ d) None of these	1
7	The second term of Taylor's series expansion of $f(x, y) = e^{xy}$ at (1,1) is a) $e$ b) $e[(x-1) + (y-1)]$ c) $\frac{e^2}{2}$ d) None of these	1
8	The minimum value of the function $f(x, y) = x^3 + y^3 - 3xy$ is a) -1    b) 1    c) 2    d) None of these	1

9	If $r = \frac{\partial^2 f}{\partial x^2}$ , $s = \frac{\partial^2 f}{\partial x \partial y}$ and $t = \frac{\partial^2 f}{\partial y^2}$ , then the condition for maxima and minima is a) $rt - s^2 < 0$ , $rt - s^2 > 0$ b) $rt - s^2 > 0$ , $rt - s^2 < 0$ c) $rt - s^2 = 0$ d) None	1
10	The value of $\frac{\partial(u,v)}{\partial(u,v)}$ is equal to a) 1    b) 0    c) 2    d) None of these	1

### Short Answer Question

Question No.	Question Description	Expected Marks
1	If $x = r \cos \theta$ , $y = r \sin \theta$ then Find the value of $J^*$ .	
2	If $x = e^u \cos v$ , $y = e^u \sin v$ Find the value of $J$ .	
3	If $x = v^2 + w^2$ , $y = w^2 + u^2$ , $z = u^2 + v^2$ Find the value of $J$ .	
4	Write Taylor's series expansion formula for $f(x, y)$ at $(a, b)$ .	
5	Write Maclaurin's series expansion formula for $f(x, y)$ .	
6	If $x = a(u + v)$ , $y = b(u - v)$ then Find the value of $J$ .	
7	Expand $f(x, y) = e^{x+y}$ by Maclaurin's theorem	
8	Find only stationary points for the function $f(x, y) = x^2 + y^2 + 6x + 12$	
9	Find only stationary points for the function $f(x, y) = x^3 + 3 - 3axy$	
10	Write the formula for volume of largest rectangular parallelepiped and greatest rectangular parallelepiped.	

### Long Answer Question

Question No.	Question Description	Expected Marks
1	If $F = xu + v - y$ , $G = u^2 + vy + w$ , $H = zu - v + vw$ , Compute $\frac{\partial(F, G, H)}{\partial(u, v, w)}$	5
2	If $x = a \cos \xi \cosh \eta$ and $y = a \sinh \xi \sin \eta$ , show that $\frac{\partial(x, y)}{\partial(\xi, \eta)} = \frac{a^2}{2} (\cosh 2\xi - \cos 2\eta)$	5
3	If $x = r \cos \theta$ , $y = r \sin \theta$ , Verify that $\frac{\partial(x, y)}{\partial(r, \theta)} \cdot \frac{\partial(r, \theta)}{\partial(x, y)} = 1$	5
4	Expand $f(x, y) = \sin x \sin y$ as far as terms of third degree.	5



5	Expand $f(x, y) = e^x \sin y$ at $(-1, \frac{\pi}{4})$ as far as terms of third degree.	5
6	Discuss the maxima and minima of function $f(x, y) = x^3 y^2 (1 - x - y)$	5
7	Find the maximum and minimum value of the function $f(x, y) = \cos x + \cos y + \cos(x + y)$	5
8	Find the minimum value of the function $f(x, y, z) = x^2 + y^2 + z^2$ when $xyz = a^3$	5
9	Find the maximum and minimum distances of the point $(3, 4, 12)$ from the sphere $x^2 + y^2 + z^2 = 1$	5
10	Find the minimum value of the function $f(x, y, z) = x^m y^n z^p$ when $x + y + z = a$	5



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Department of Basic Sciences and Humanities

### QUESTION BANK

Title of the Subject: Engineering Mathematics-I		
Title of the Unit: Reduction Formulae and Curve Tracing	Unit No:- 4	

Multiple Choice Questions		
Question No.	Question Description	Expected Marks
1	$\int_0^{\frac{\pi}{2}} \sin^2 x \cdot dx = \dots$ a) $\frac{\pi}{4}$ b) 0    c) 2    d) None of these	1
2	A curve $xy = c$ is symmetric about a) Y-axis    b) $Y = X$ c) X-axis    d) $X = 2a$	1
3	The equation of the asymptote to the curve $y = \frac{x}{(1+x^2)}$ is	1

	a) $x = 0$ b) $x = \pm 1$ c) $y = 0$ d) $y = x$	
4	The curve $x = a \cos^3 \theta, y = a \sin^3 \theta$ is symmetric about a) Y-axis      b) $Y = X$ c) X-axis      d) $X=a$	1
5	The curve $r = a \sin 3\theta$ , is symmetrical about a) Initial line      b) Pole      c) $\theta = \pi$ d) $\theta = \pi/2$	1
6	The equation of the tangents at origin for the curve $y^2(a-x) = x^3$ is/are a) $x = 0$ b) $y = 0$ c) $x = 0, y = 0$ d) $x = a$	1
7	Find $\frac{dy}{dx}$ at $\theta = 0$ , for the curve $x = a(\theta + \sin \theta), y = a(1 - \cos \theta)$ a) 1      b) -1      c) 0      d) $\infty$	1
8	Find the point of intersections with X-axis for the curve $y^2(4-x) = x(x-2)^2$ is/are a) (0,0)      b) (0,2)      c) (0,4)      d) (0,0) and (0,2)	1
9	For the curve $a^2 x^2 = y^3(2a-y)$ at the origin is a) Node point      b) singular point      c) Cusp point      d) $y = \pm a$	1
10	The equation of the asymptote to the curve $y^2(x^2-1) = x$ is a) $x = 0$ b) $x = \pm 1$ c) $y = 0$ d) $X=2a$	1

### Short Answer Question

Question No.	Question Description	Expected Marks
1	Find the asymptote to curve $a^2 x^2 = y^2(x^2 + a^2)$ .	2
2	Find the region of existence to curve $x^2(2a-y) = y^3$	2
3	The curve $x^{\frac{1}{2}} + y^{\frac{1}{2}} = a^{\frac{1}{2}}$ is symmetric about .....	2
4	1) Find the asymptote to curve $x y^2 = 4a^2(2a-x)$ .	2
5	The curve $x = a \cos t, y = a \sin t$ is symmetric about.....	2

6	Find the points of intersection of the curve $a^2x^2 = y^3(2a - y)$	2
7	The curve cycloid $x = a(\theta + \sin\theta), y = a(1 + \cos\theta)$ is symmetric about .....	2
8	Find the region of existence to curve $y^2(a + x) = x^2(a - x)$ .	2
9	Evaluate: $\int_0^{\frac{\pi}{2}} \sin^3 \theta \cos^4 \theta . d\theta$	2
10	Evaluate: $\int_0^{\frac{\pi}{4}} \sin^4 2x \, dx$	2

Long Answer Question		
Question No.	Question Description	Expected Marks
1	Trace the curve $a^4y^2 = x^2(a^2 - x^2)$ with full justification	5
2	Trace the curve $y^2(x + a) = x^2(3a - x)$ .	5
3	Trace the cycloid $x = a(\theta + \sin\theta), y = a(1 - \cos\theta)$ .	5
4	Trace the curve $y = c \cosh\left(\frac{x}{c}\right)$	5
5	Trace the curve $y(x^2 + 4a^2) = 8a^3$	5
6	Trace the curve $xy^2 = 4a^2(2a - x)$ .	5
7	Trace the curve $y^2(a^2 - x^2) = x^2(a^2 + x^2)$	5
8	Trace the curve $x^{\frac{1}{2}} + y^{\frac{1}{2}} = a^{\frac{1}{2}}$	5

9	Evaluate : $\int_0^{\pi} x \sin^5 x \cos^4 x \, dx$	5
10	Evaluate: $\int_0^{\frac{\pi}{2}} \frac{\sin^4 \theta}{(1+\cos \theta)^2} \cdot d\theta$	5



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### QUESTION BANK

Title of the Subject: Engineering Mathematics-I	
Title of the Unit: Multiple Integrals	Unit No:- 5

Multiple Choice Questions		
Question No.	Question Description	Expected Marks
1	$\int_1^2 \int_0^x dx \cdot dy = \dots \dots$ a) $\frac{3}{2}$ b) $\frac{1}{2}$ c) $-1$ d) $3$	1
2	Area of the closed region bounded by two Cartesian curves is given by, a) Area= $\int \int dx \, dr$ b) Area= $\int \int dx \, dy$ c) Area= $\int \int x \, dx \, dy$ d) None of these	1
3	The polar form of the integral. $\int_y^u \int_0^u dx \cdot dy$ is. a) $\int_0^{\frac{\pi}{2}} \int_0^{a \cos \theta} r \cdot dr \cdot d\theta$ b) $\int_0^{\frac{\pi}{4}} \int_0^{a \cos \theta} r \cdot dr \cdot d\theta$ c) $\int_0^{\frac{\pi}{4}} \int_0^{a \sec \theta} r \cdot dr \cdot d\theta$ d) None of these	1
4	$\int_1^2 \int_0^{3y} y \cdot dx \cdot dy = \dots \dots$ a) $3$ b) $5$ c) $7$ d) $9$	1

5	For $\int_0^\infty \int_x^\infty f(x,y) dx dy$ by change of order of integration we get, a) $\int_x^\infty \int_0^\infty f(x,y) dx dy$ b) $\int_0^\infty \int_0^x f(x,y) dx dy$ c) $\int_0^\infty \int_0^y f(x,y) dx dy$ d) $\int_0^\infty \int_0^\infty f(x,y) dx dy$	1
6	For $\int_0^a \int_0^y f(x,y) dx dy$ , the change of order is a) $\int_0^y \int_0^a f(x,y) dx dy$ b) $\int_0^a \int_x^a f(x,y) dx dy$ c) $\int_0^a \int_a^x f(x,y) dx dy$ d) $\int_0^a \int_a^y f(x,y) dx dy$	1
7	Area of the closed region bounded by two Polar curves is given by, a) Area = $\int \int dr d\theta$ b) Area = $\int \int dx dy$ c) Area = $\int \int x dr d\theta$ d) None of these	1
8	$\int_0^{\frac{\pi}{2}} \int_0^{\sin \theta} r dr d\theta = \dots \dots$ a) $\frac{\pi}{2}$ b) $\frac{\pi}{4}$ c) $\frac{\pi}{8}$ d) 0	1
9	$\int \int dx dy$ gives a) Area of region b) Perimeter of region c) Volume of a region d) None of these	1
10	The value of integral $\int_0^1 \int_0^2 \int_0^3 x^2 dx dy dz$ is a) 2/3    b) 4/3    c) 3/2    d) 1/3	1

### Short Answer Question

Question No.	Question Description	Expected Marks
1	Evaluate $\int_0^1 \int_0^y x dx dy$	2
2	Show the region of integration for $\int_0^1 \int_x^{x^2} f(x,y) dx dy$	2
3	Change the order of integration $\int_0^1 \int_0^x f(x,y) dx dy$	2
4	Evaluate $\int_0^\pi \int_0^{\sin \theta} r^3 dr d\theta$	2
5	Evaluate $\int_0^1 \int_0^x \int_0^{x-y} dx dy dz$	2
6	Find the limits of inner and outer integral of $\int \int x^2 y^2 dx dy$ over the first quadrant of the circle $x^2 + y^2 = 4$ .	2
7	Evaluate $\int_0^1 \int_0^2 \int_0^3 xyz dx dy dz$	2

8	Shade the region of integration for $\int_0^1 \int_0^x f(x, y) \cdot dx dy$	2
9	Change the integration in polar form: $\int_0^a \int_0^{\sqrt{a^2-x^2}} \sin \left[ \frac{\pi}{a^2} (a^2 - x^2 - y^2) \right] dx dy$	2
10	Evaluate : $\int_0^\pi \int_0^a r \sin \theta dr d\theta$	2

Long Answer Question		
Question No.	Question Description	Expected Marks
1	Evaluate: $\int \int xy dx dy$ over the area bounded by parabola $y = x^2$ & $y^2 = -x$	5
2	Evaluate $\int \int (x^2 - y^2) dx dy$ over the area of the triangle whose vertices are at the points (0,1), (1,1) & (1,2).	5
3	Evaluate $\int \int r^2 dr d\theta$ between the circles: $r = 2 \sin \theta$ & $r = 4 \sin \theta$ .	5
4	Evaluate by changing to polar form $\int_0^{\frac{\pi}{\sqrt{2}}} \int_y^{\sqrt{a^2-y^2}} \log(x^2 + y^2) dx dy$ ; ( $a > 0$ )	5
5	Change the order of integration : $\int_0^a \int_0^{\frac{a^2}{x}} f(x, y) dx dy$	5
6	Express the following double integral as a single term integral & hence evaluate: $\int_{-3}^2 \int_{2-y}^b dx dy + \int_2^7 \int_{y-2}^b dx dy$	5
7	Change the order of integration: $\int_0^2 \int_{1-y}^{1+y} f(x, y) dx dy$	5
8	Evaluate $\int_0^{\log 2} \int_0^x \int_0^{x+y} e^{x+y+z} dx dy dz$	5
9	Evaluate : $\int \int \int \frac{dx dy dz}{(x+y+z+1)^3}$ over the volume of tetrahedrons bounded by coordinate planes & the plane $x + y + z = 7$	5
10	Evaluate $\int_{-1}^1 \int_0^x \int_{x-z}^{x+z} (x + y + z) dx dy dz$	5